

#### Find the derivatives using power rule:

$$y = 10x^3$$

$$y = \frac{1}{2}x^{-2}$$

$$y = \frac{1}{2\sqrt{x}}$$

$$y=3x^{\frac{-1}{15}}$$

$$y = 8x^6 + 2x^{17}$$

$$y = \sqrt[5]{x}$$

$$y = x^{\frac{1}{31}} + x^{\frac{-1}{7}}$$

$$y = \frac{5}{3}x^3 - \frac{7}{6}x^6 + \frac{6}{4}x^8$$

$$y = \frac{1}{2}x^{\frac{3}{2}} - \frac{22}{7}x^{\frac{-5}{2}} + x^{\frac{3}{7}}$$

 $y = 2x^{12} + 6x^7 + x^4$ 

Ex 1: Starting today a table is being sold at Jaime's furniture store for \$345. This is 69% of its regular price. What was the price yesterday?

Let 
$$x = \text{price yesterday}$$
  
\$345 \(\frac{15}{15}\) \(\frac{69\%}{69}\) \(\frac{0f}{69}\) \(\times\)
$$\frac{345}{69} = \frac{.69 \times .69}{.69}$$

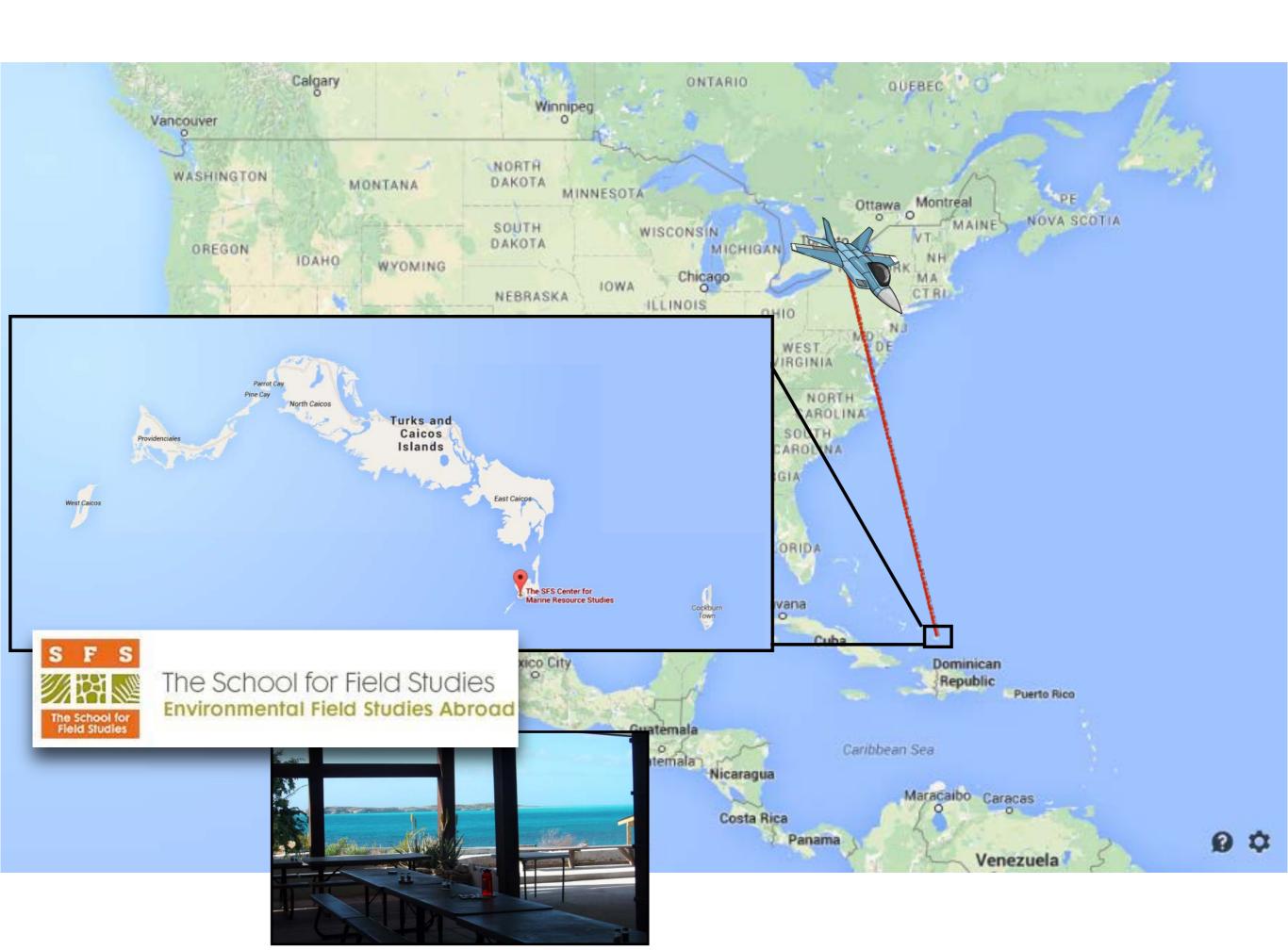
$$\times = \frac{345}{69} = \frac{.345}{.69} = 31$$

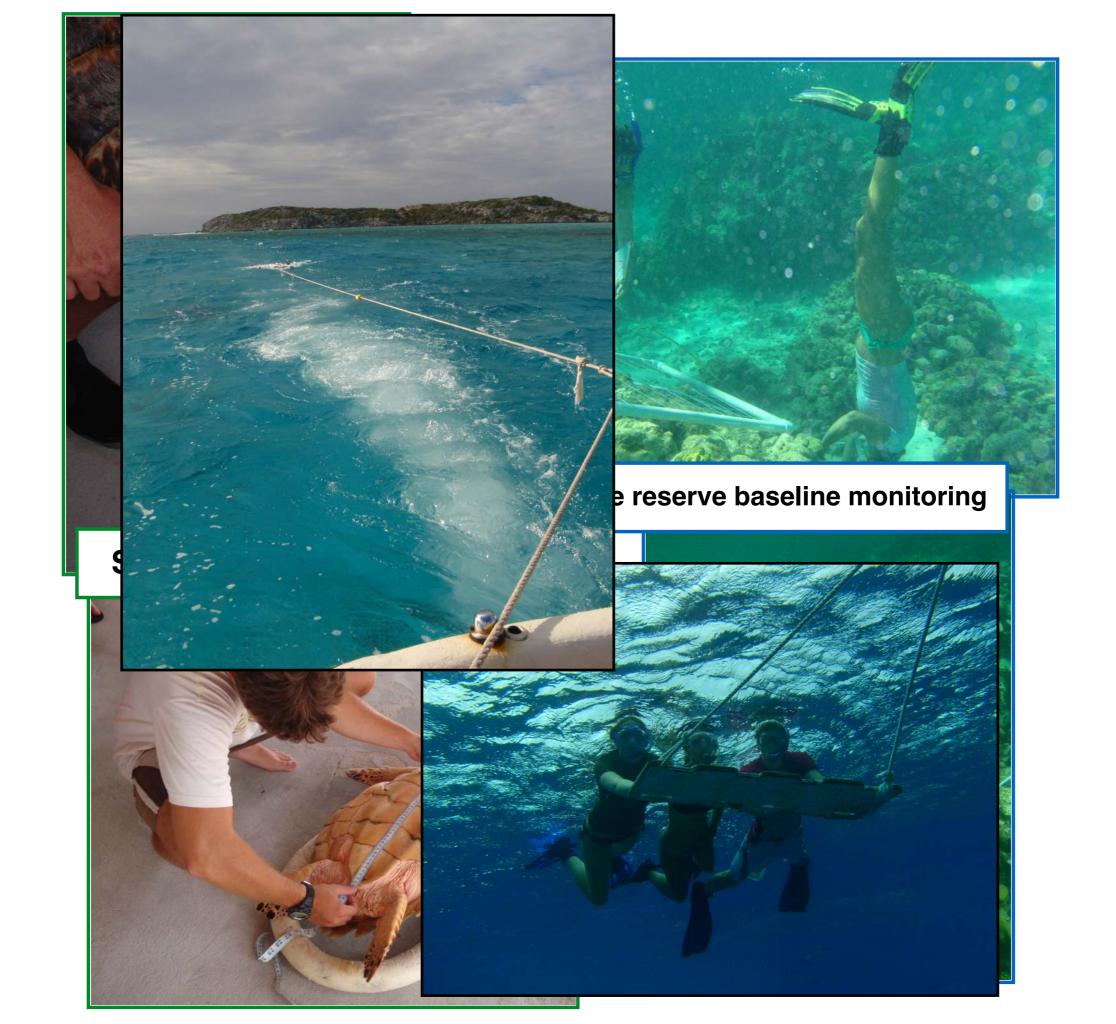


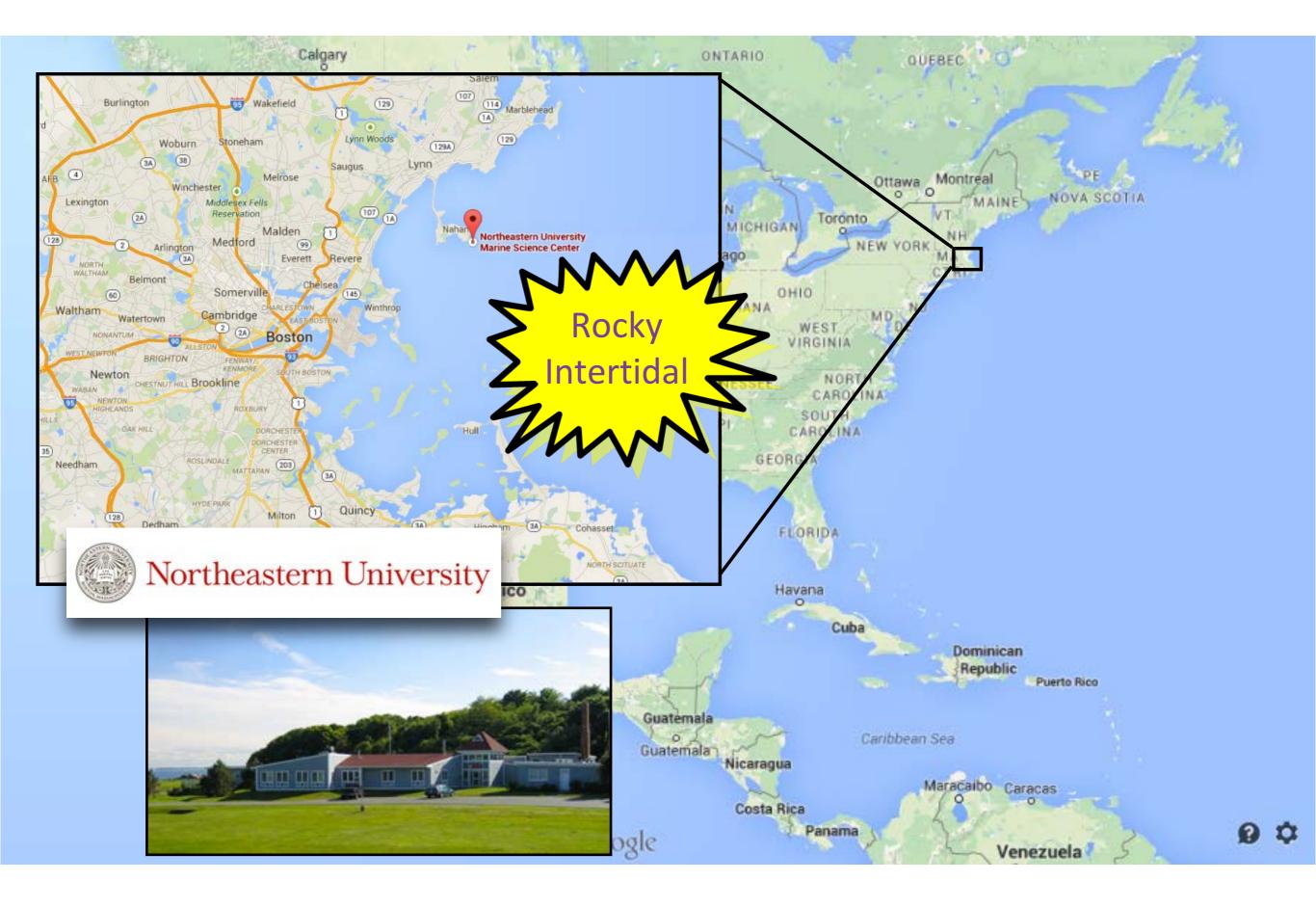
All other teachers



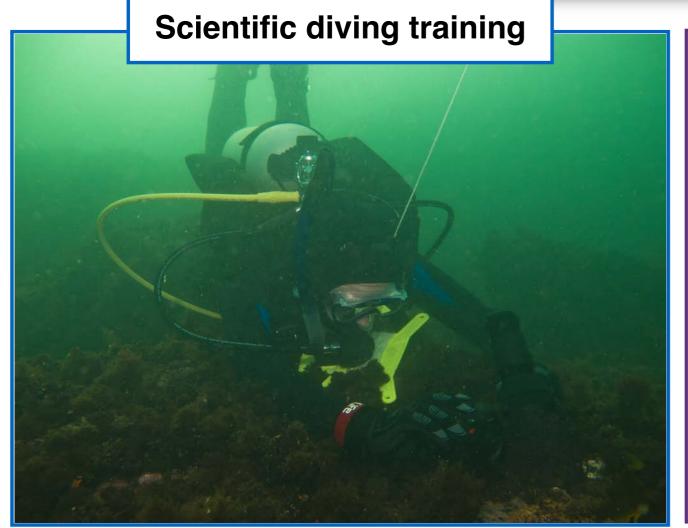
Math teacher

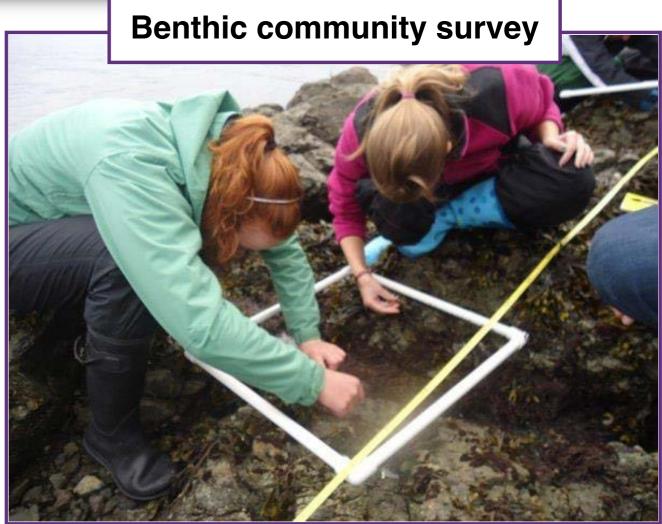


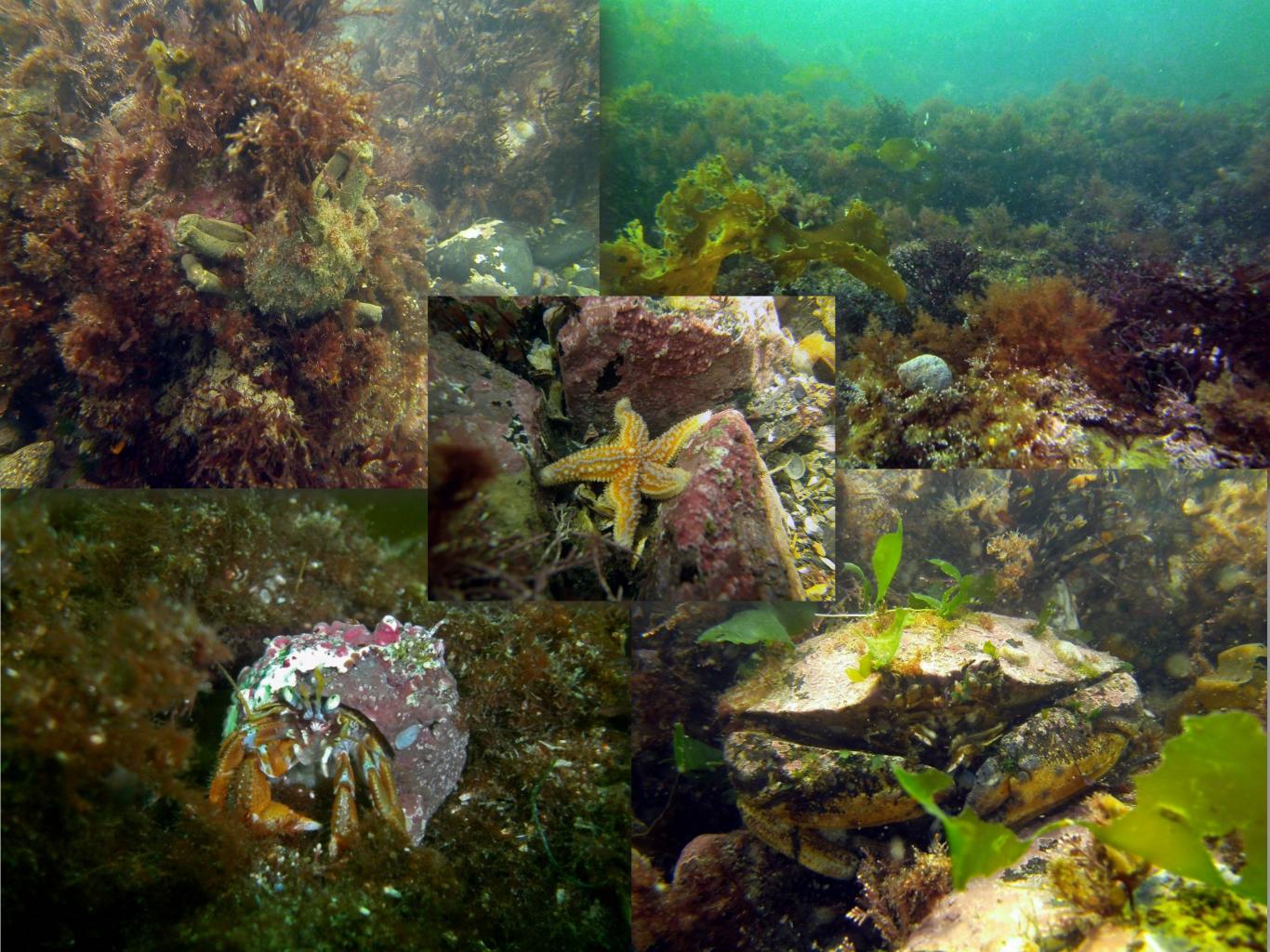




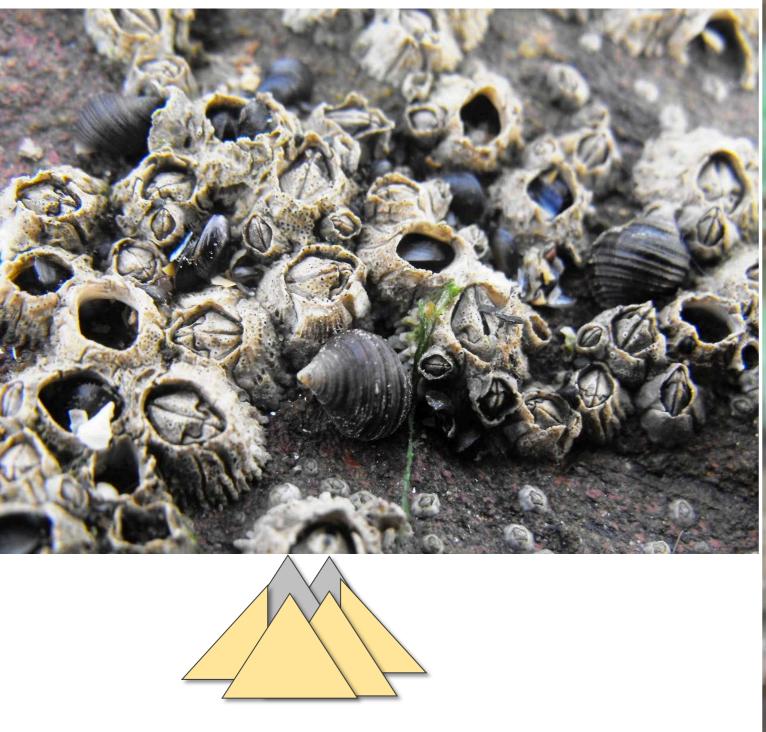






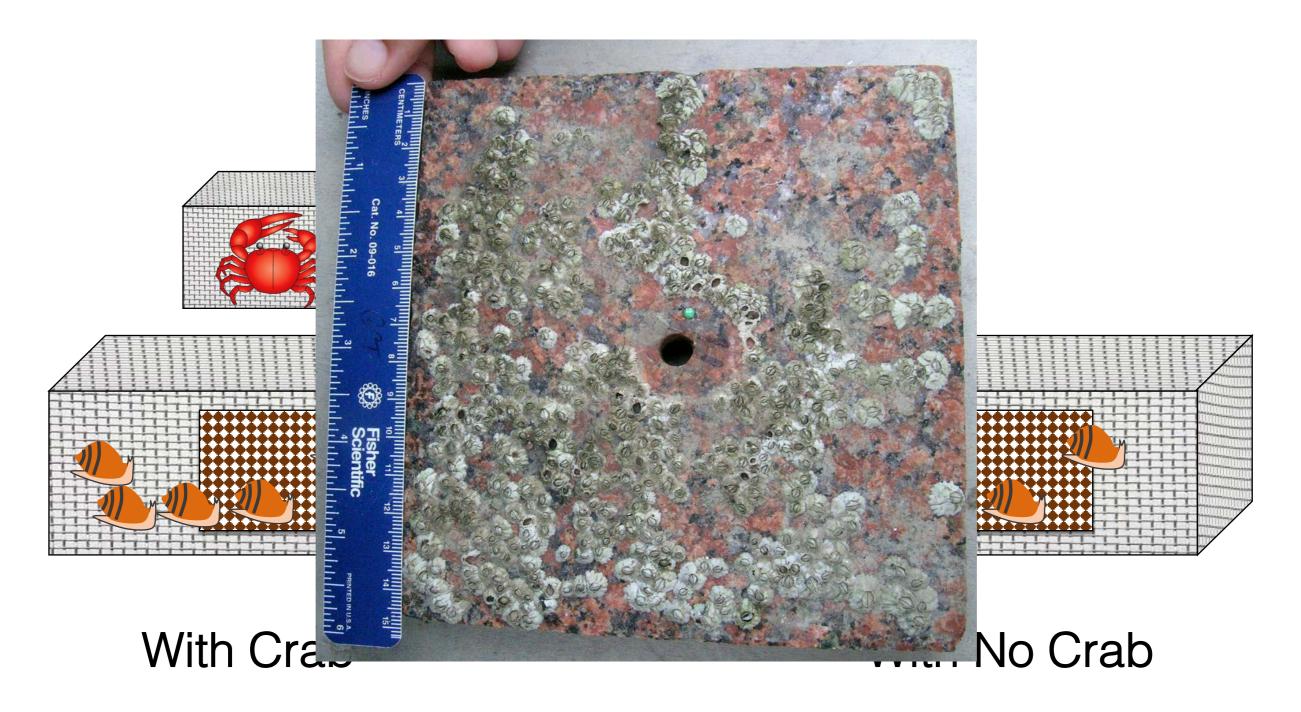


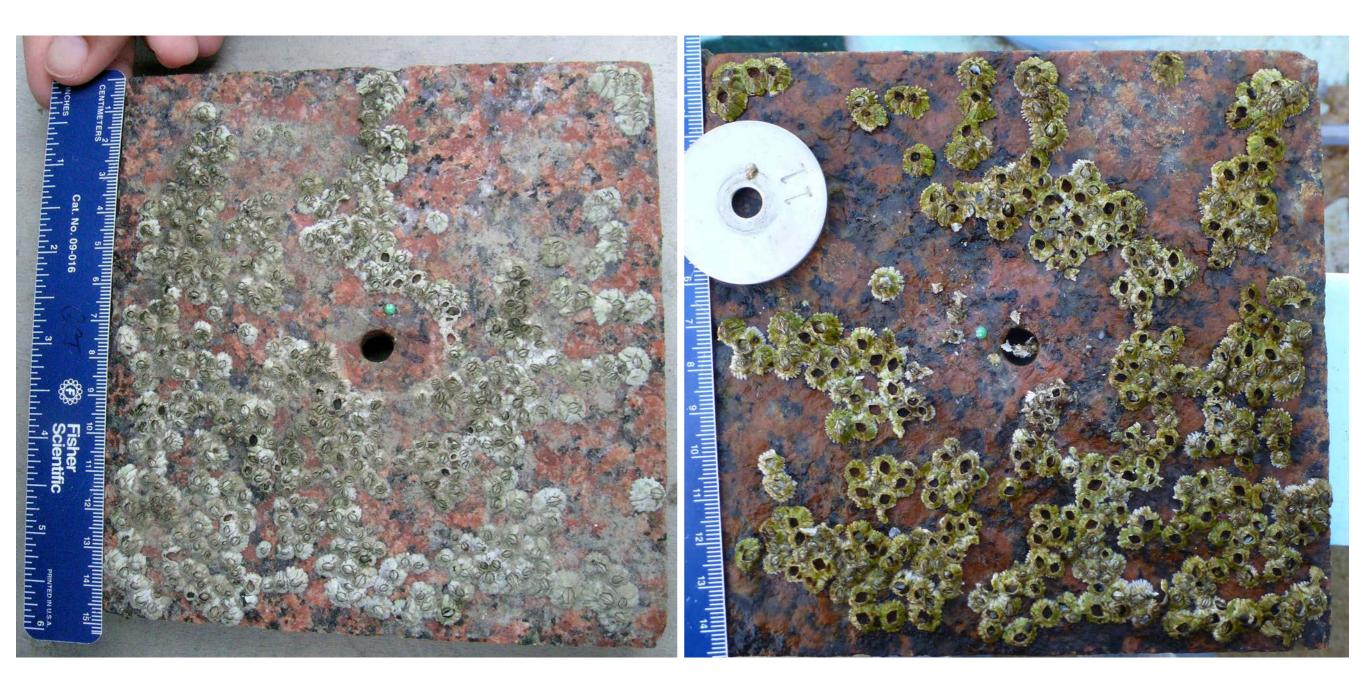
# ECOLOGY C





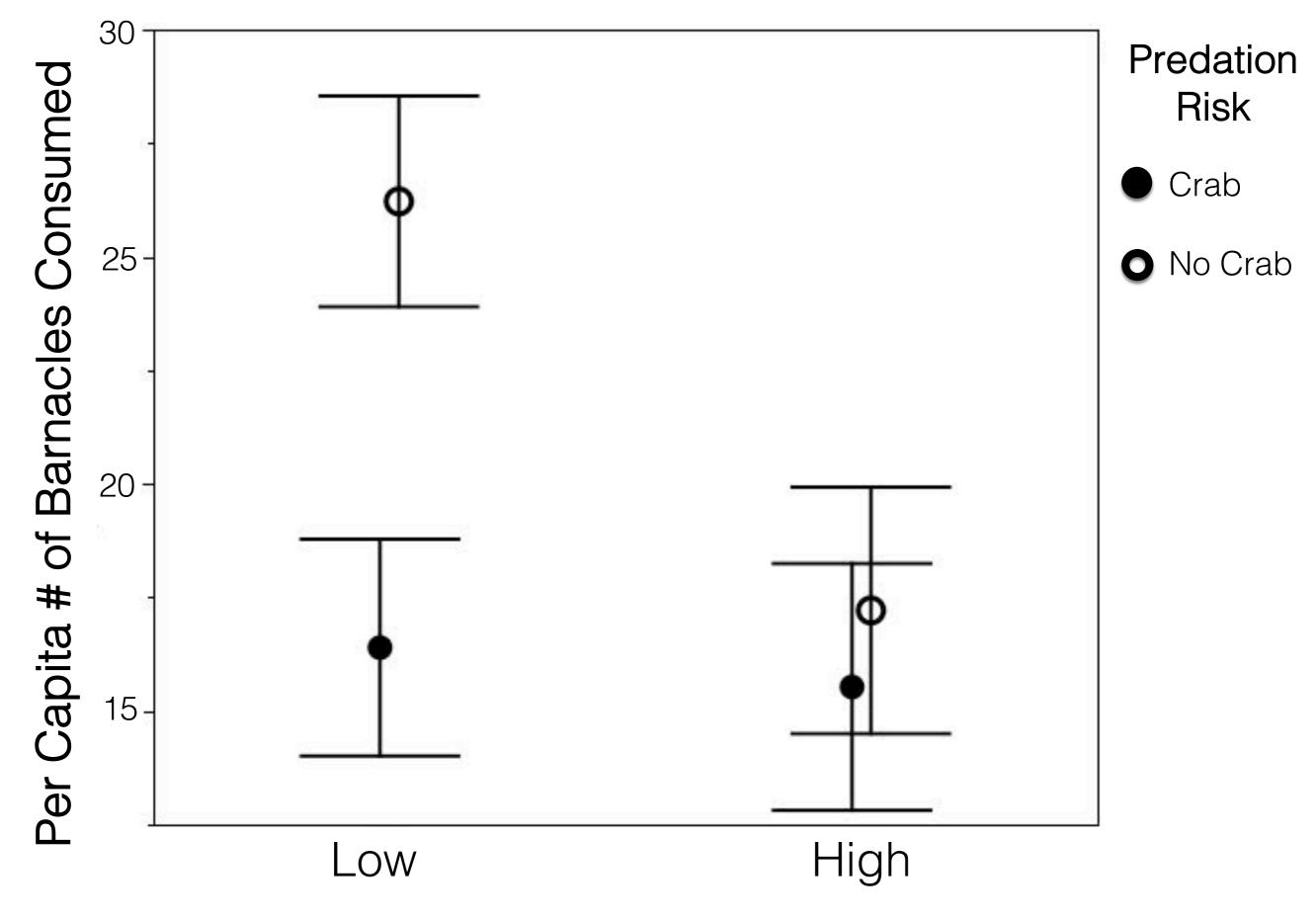
# ECOLOGY OF FEAR





Initial Final

Barnacle Cover



Intertidal Elevation





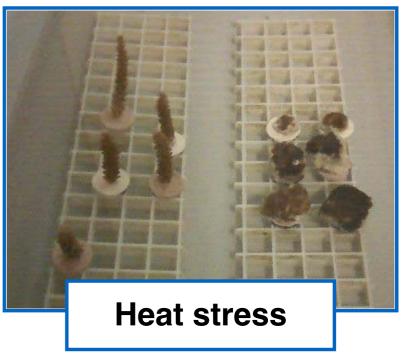
### **White Band Disease**



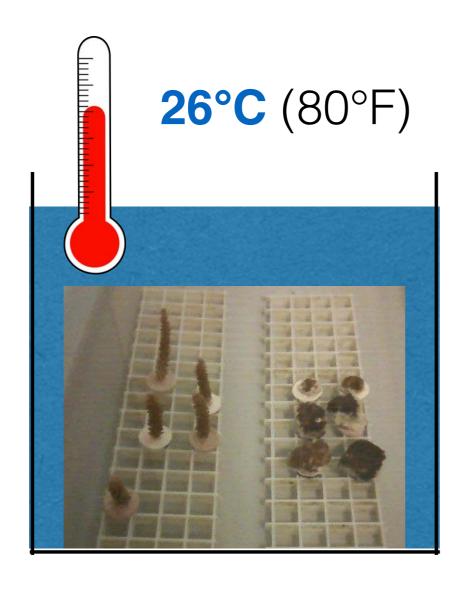


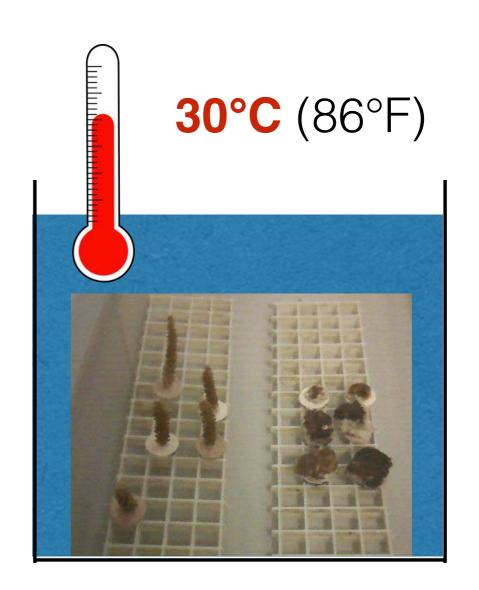






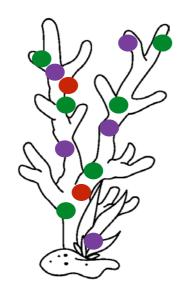
**Microbial community** 

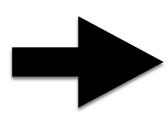


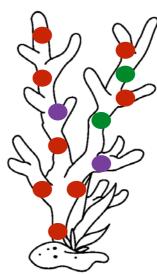


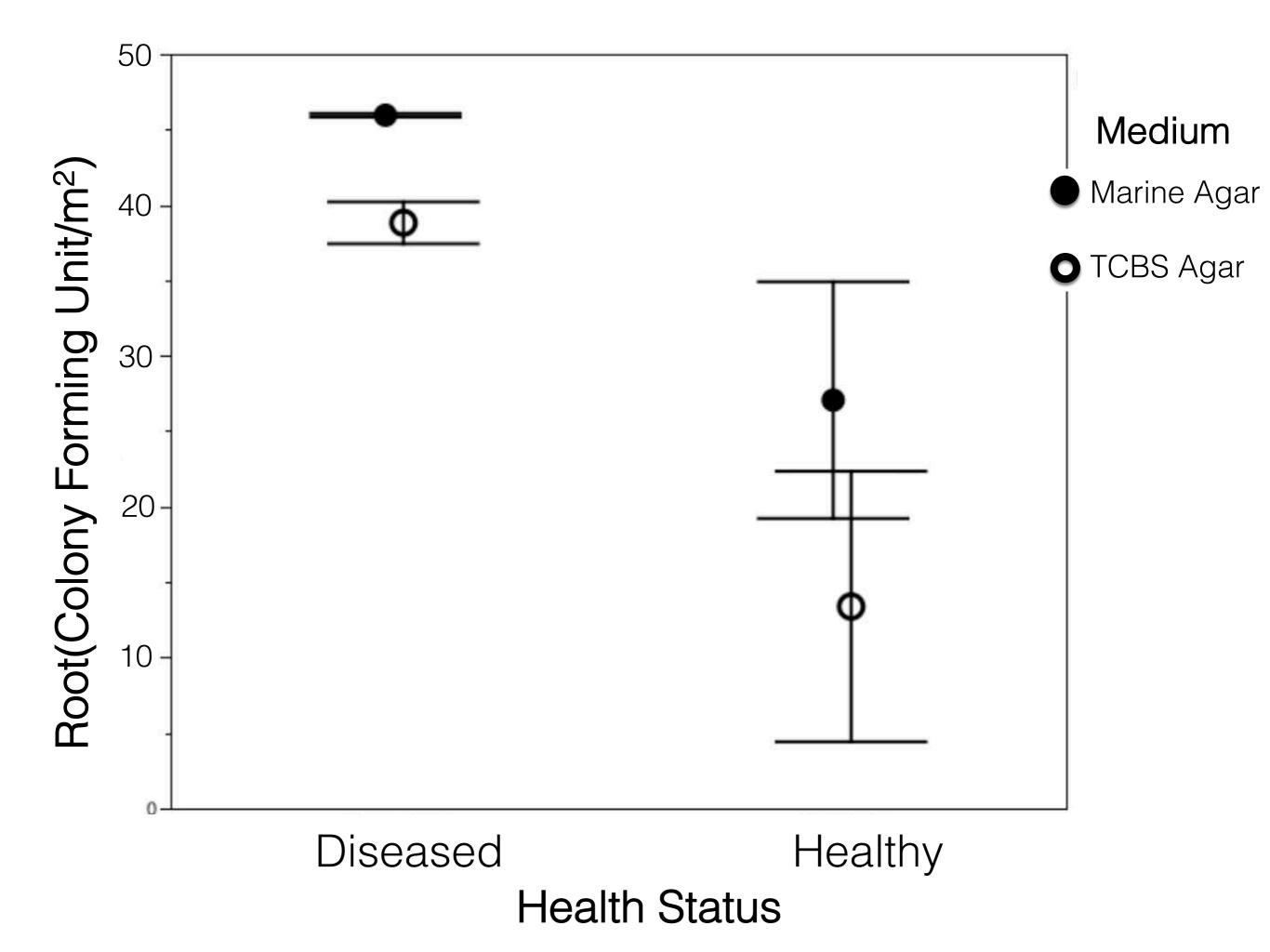
**Ambient** 



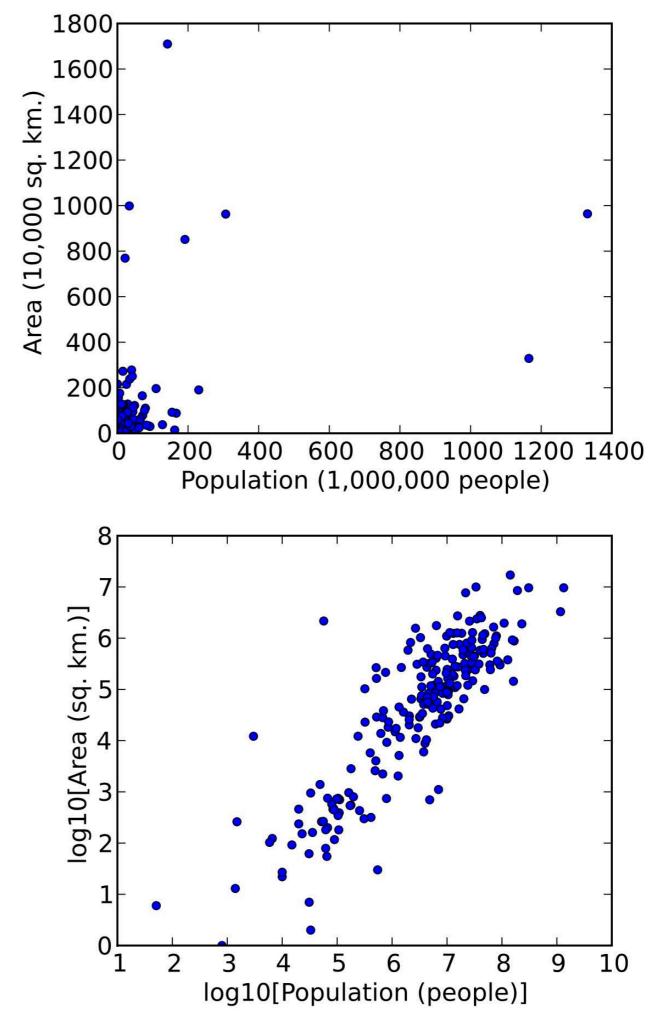




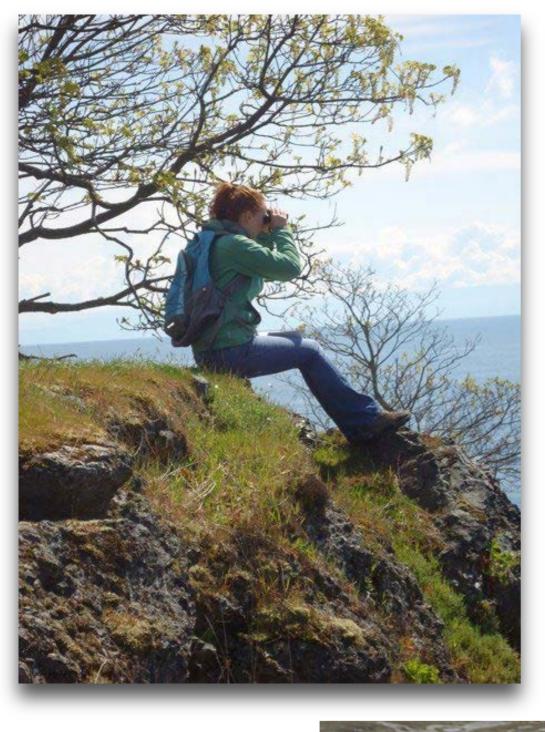




Transformed data allow us to see data clearly and detect patterns















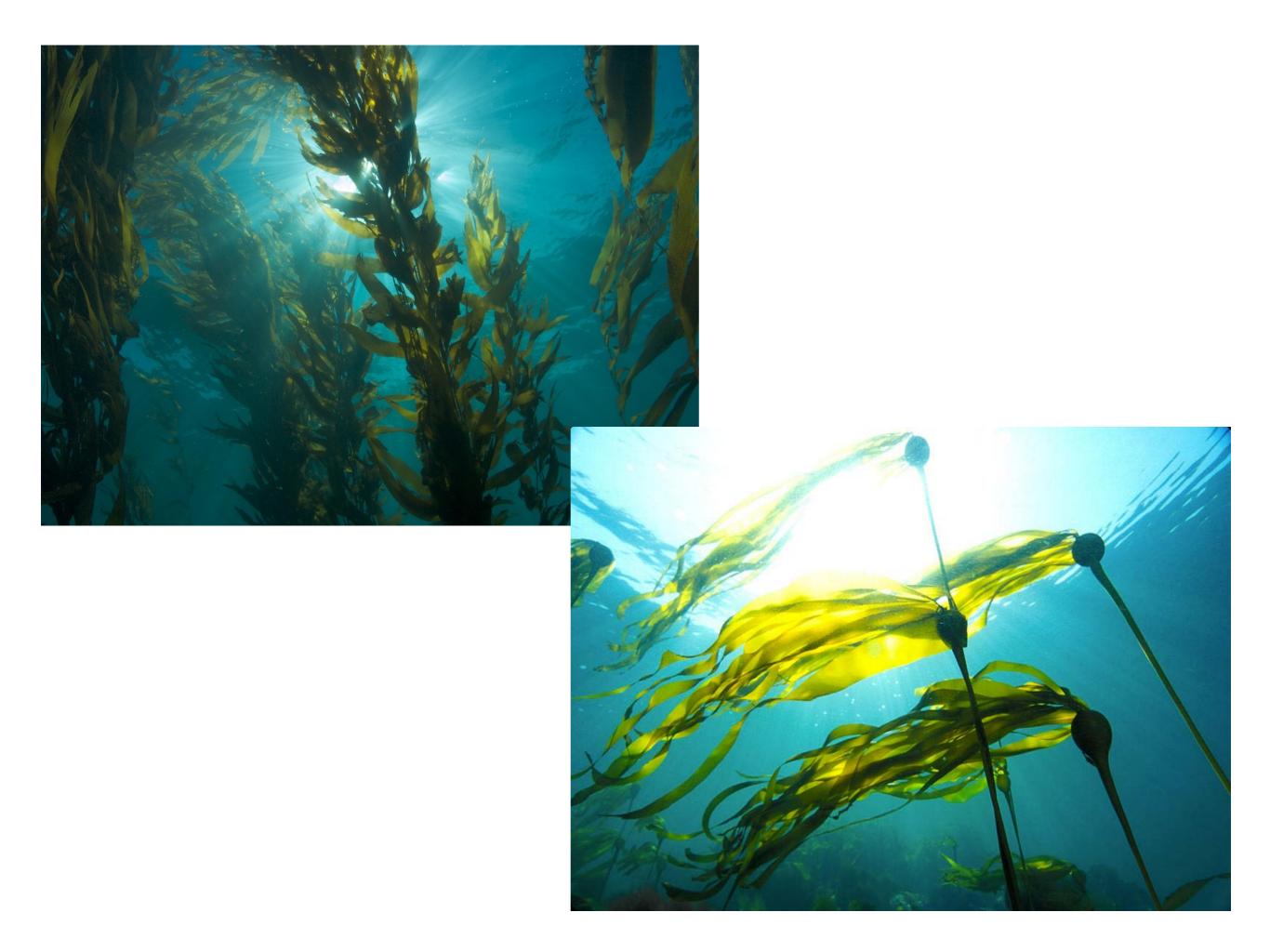


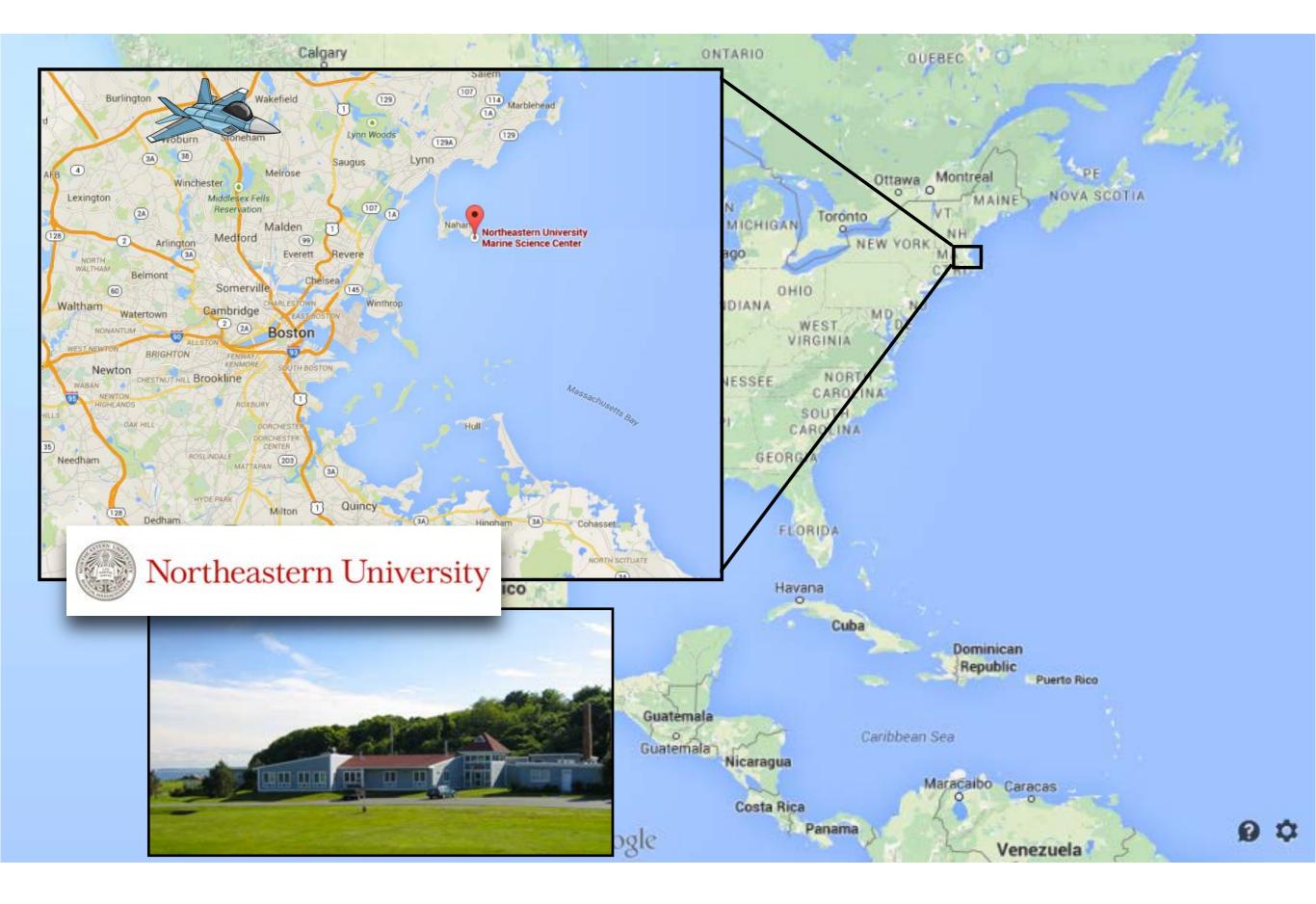












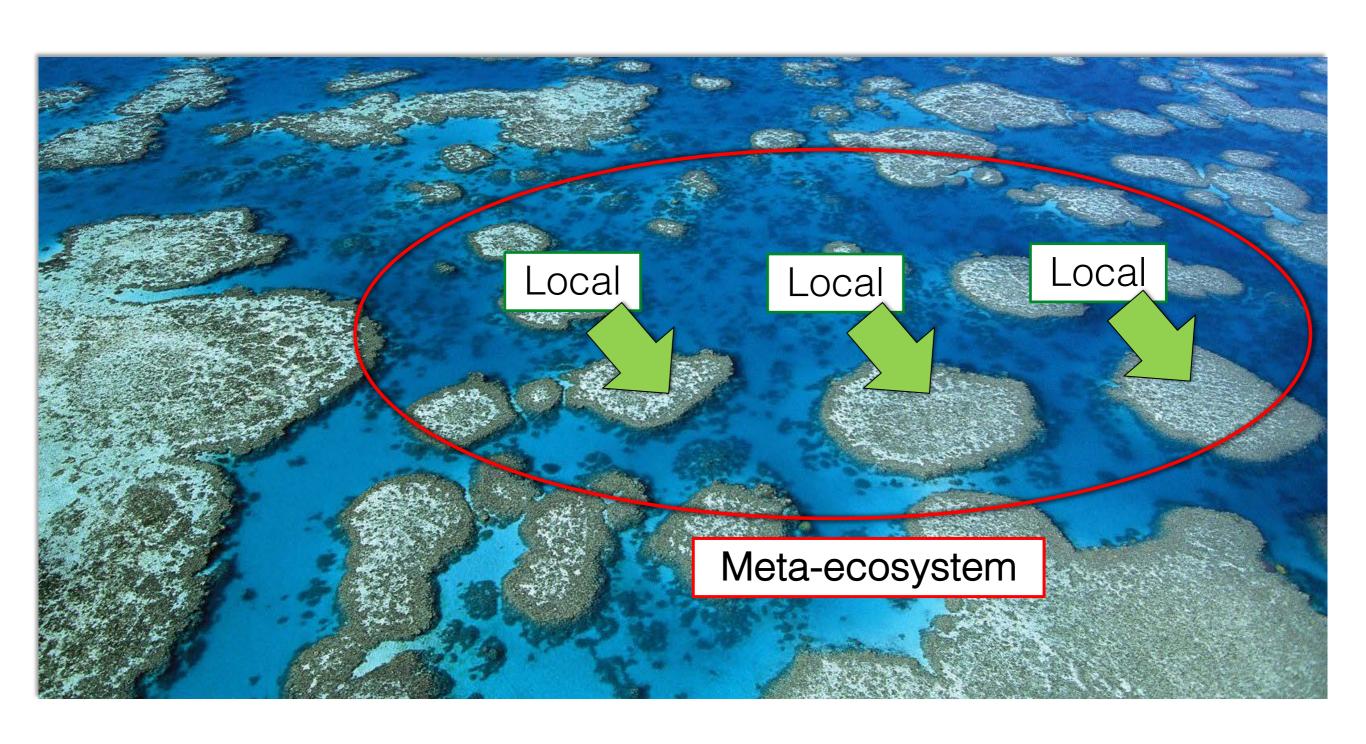
#### Reciprocal feedbacks between spatial subsidies and reserve networks in coral reef meta-ecosystems

BARBARA SPIECKER, <sup>1</sup> TARIK C. GOUHIER, <sup>1,3</sup> AND FRÉDÉRIC GUICHARD<sup>2</sup>

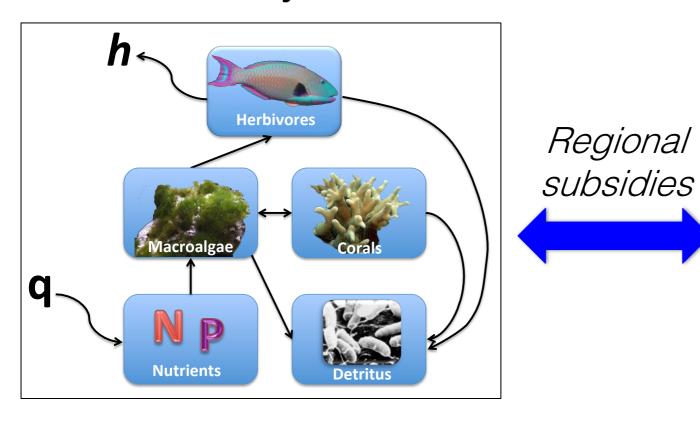
<sup>1</sup>Marine Science Center, Northeastern University, 430 Nahant Road, Nahant, Massachusetts, 01908, USA <sup>2</sup>Department of Biology, McGill University, 1205 Avenue Docteur Penfield, Montréal, Québec, H3A1B1, Canada

Top-down processes such as predation and herbivory have been shown to control the dynamics of communities across a range of ecosystems by generating trophic cascades. However, theory is only beginning to describe how these local trophic processes interact with spatial subsidies in the form of material (nutrient, detritus) transport and organismal dispersal to (1) shape the structure of interconnected (meta-) ecosystems and (2) determine their optimal management via reserve networks. Here, we develop a metaecosystem model to understand how the reciprocal feedbacks between spatial subsidies and reserve networks modulate the importance of top-down control in a simple herbivorous fish-macroalgae-coral system. We show that in large and isolated reserve networks where connectivity between protected and unprotected areas is limited, spatial subsidies remain largely confined to reserves. This retention of spatial subsidies promotes the top-down control of corals and macroalgae by herbivores inside reserves but reduces it outside reserves. Conversely, in small and aggregated reserves where connectivity between protected and unprotected areas is high, the spillover of spatial subsidies causes a reduction in topdown control of corals and macroalgae by herbivores inside reserves and an increase in the strength of top-down control outside reserves. In addition, we demonstrate that there is a trade-off between local and regional conservation objectives when designing reserve networks: small and aggregated reserves based on the extent of dispersal maximize the abundance of corals and herbivores regionally, whereas large and isolated reserves always maximize the abundance of corals within reserves, regardless of the extent of dispersal. The existence of such "conservation traps," which arise from the fulfillment of populationlevel objectives within local reserves at the cost of community-level objectives at regional scales, suggests the importance of adopting a more holistic strategy to manage complex and interconnected ecosystems.

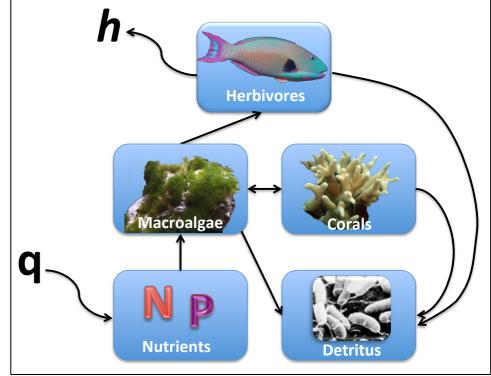
Key words: corals; dispersal; material transport; meta-ecosystem; reserve networks; spatial management; spatial subsidies; top-down control; trophic cascades



### Local ecosystem *x*



# Local ecosystem y



### Modeling local and regional dynamics using integro-differential equations

Regional process

Local process



$$\frac{dH(x)}{dt} = \frac{aM(x)H(x)}{1 + avM(x)} - m_H H(x) - h(x)H(x) - d_H H(x) + \int_{-\frac{L}{2}}^{\frac{L}{2}} d_H(y)\kappa_H(x - y) \, dy$$



$$\frac{\mathrm{d}C(x)}{\mathrm{d}t} = \left[\int_{-\frac{L}{2}}^{\frac{L}{2}} r_C C(y) \kappa_C(x - y) \mathrm{d}y\right] \left(1 - M(x) - C(x)\right) - m_C C(x)$$



$$\frac{dM(x)}{dt} = \left[ \int_{-\frac{L}{2}}^{\frac{L}{2}} \frac{r_M N(y)}{1 + k N(y)} M(y) \kappa_M(x - y) dy \right] (1 - M(x) - C(x)) - m_M M(x) - \frac{aM(x)H(x)}{1 + avM(x)}$$



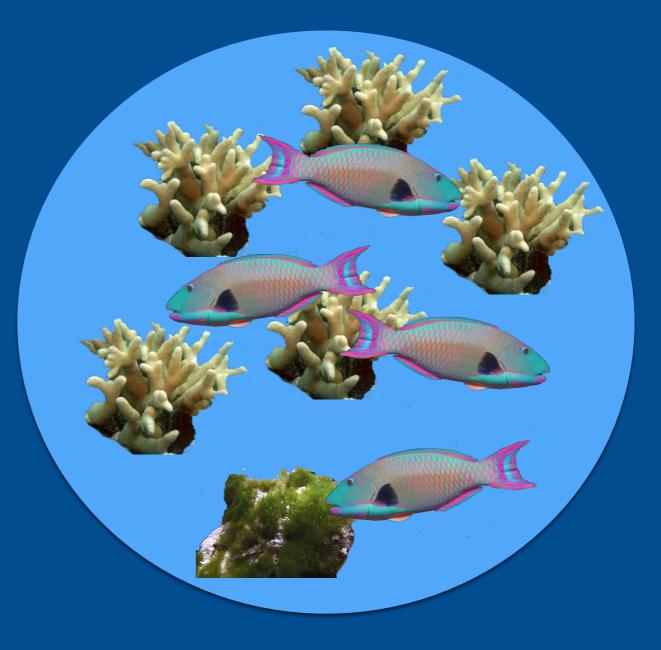
$$\frac{dD(x)}{dt} = m_M M(x) + m_H H(x) + m_C C(x) - \gamma D(x) - d_D D(x) + \int_{-\frac{L}{2}}^{\frac{L}{2}} d_D(y) \kappa_D(x - y) dy$$

$$\frac{dN(x)}{dt} = q - \epsilon N(x) + f\gamma D(x) - \frac{r_M N(x)}{1 + kN(x)} M(x) - d_N N(x) + \int_{-\frac{L}{2}}^{\frac{L}{2}} d_N(y) \kappa_N(x - y) dy$$

```
📝 Editor – /Users/barbaraspiecker/Documents/Academia/Research/NU Research/MATLAB/metaecosystem_analysis/determine_local_stability_met... 🕤 🖽 🗴
   place reserves.m × run place reserves.m ×
                                             determine local stability metaecosystem 1D.m × +
         function [equi, abundS, abundM1, abundN1, abundC, abundM2, abundN2, mapVals] = ...
  1
  2
             determine_local_stability_metaecosystem_1D (rSval, mSval, rMval, mMval, rCval, mCval, betaval, q1val, q2val, eps1val, eps2v
         global S C M1 M2 N1 N2 eps1 eps2 rM rC rS g1 g2 mM mC mS d beta;
  3 -
         syms S C M1 M2 N1 N2 gam eps1 eps2 rM rC rS g1 g2 mM mC mS d beta;
  4 -
  5 -
         model=[rS*S*(1-S-M1)-mS*S; ...
  6
             rM*N1*M1*(1-S-M1)-mM*M1; ...
  7
             d*(eps2*N2-eps1*N1)+q1-eps1*N1-rM*M1*N1; ...
  8
             rC*C*(1-C-M2)-mC*C: ...
             rM*N2*M2*(1-C-M2)-mM*M2-beta*M2; ...
  9
 10
             d*(eps1*N1-eps2*N2)+q2-eps2*N2-rM*M2*N2];
         sol=solve(model, S, M1, N1, C, M2, N2);
 11 -
 12
 13
         % Number of solutions
 14 -
         nsol=length(sol.C);
 15
         % Jacobian matrix used to compute local stability
 16
         v=[S, M1, N1, C, M2, N2];
 17 -
 18 -
         jacGenericTemplate=jacobian(model, v);
 19
 20 -
         mapVals=nan(length(betaval),1);
         abundS=nan(length(betaval),1);
 21 -
         abundM1=nan(length(betaval),1);
 22 -
         abundN1=nan(length(betaval),1);
 23 -
 24 -
         abundC=nan(length(betaval),1);
 25 -
         abundM2=nan(length(betaval),1);
         abundN2=nan(length(betaval),1);
 26 -
 27
         % Equilibrium states
 28
         equi.DensSUnstable=nan(nsol, length(betaval));
 29 -
         equi.DensM1Unstable=nan(nsol, length(betaval));
 30 -
         Agui DancMillnetahla-nan(neal langth(hataval)).
```

## Large, isolated reserve





outside reserve

inside reserve

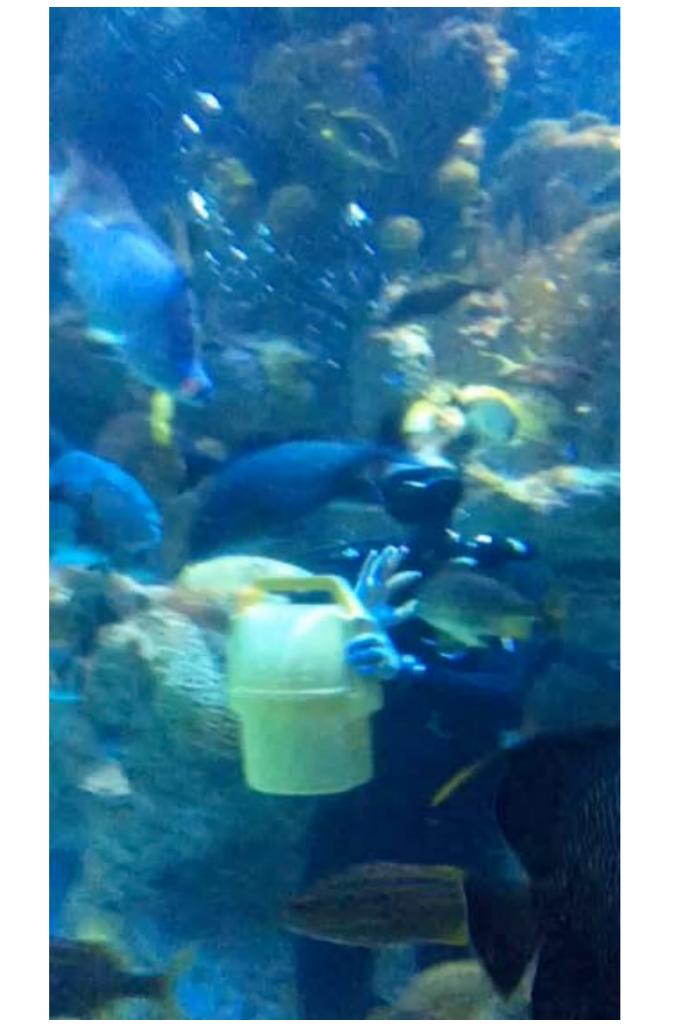
# Small, aggregated reserves







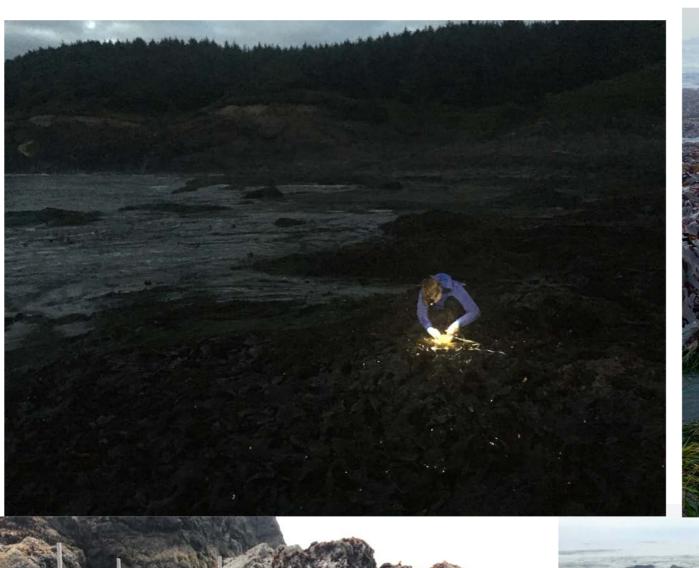






### When you are in the water and seaweed touches your leg

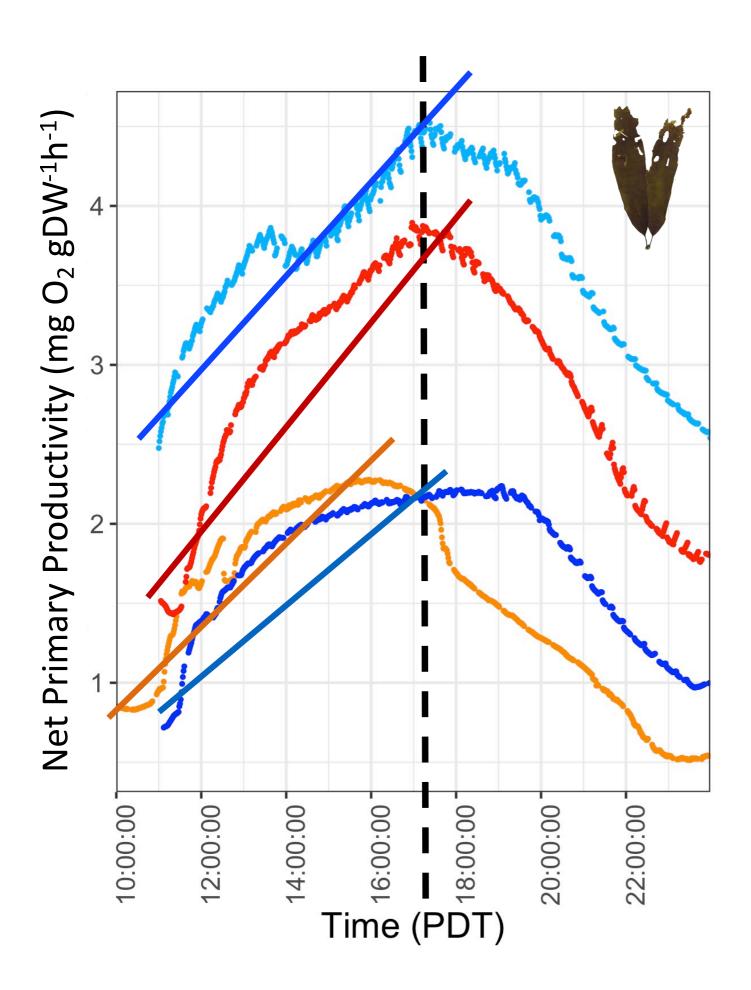






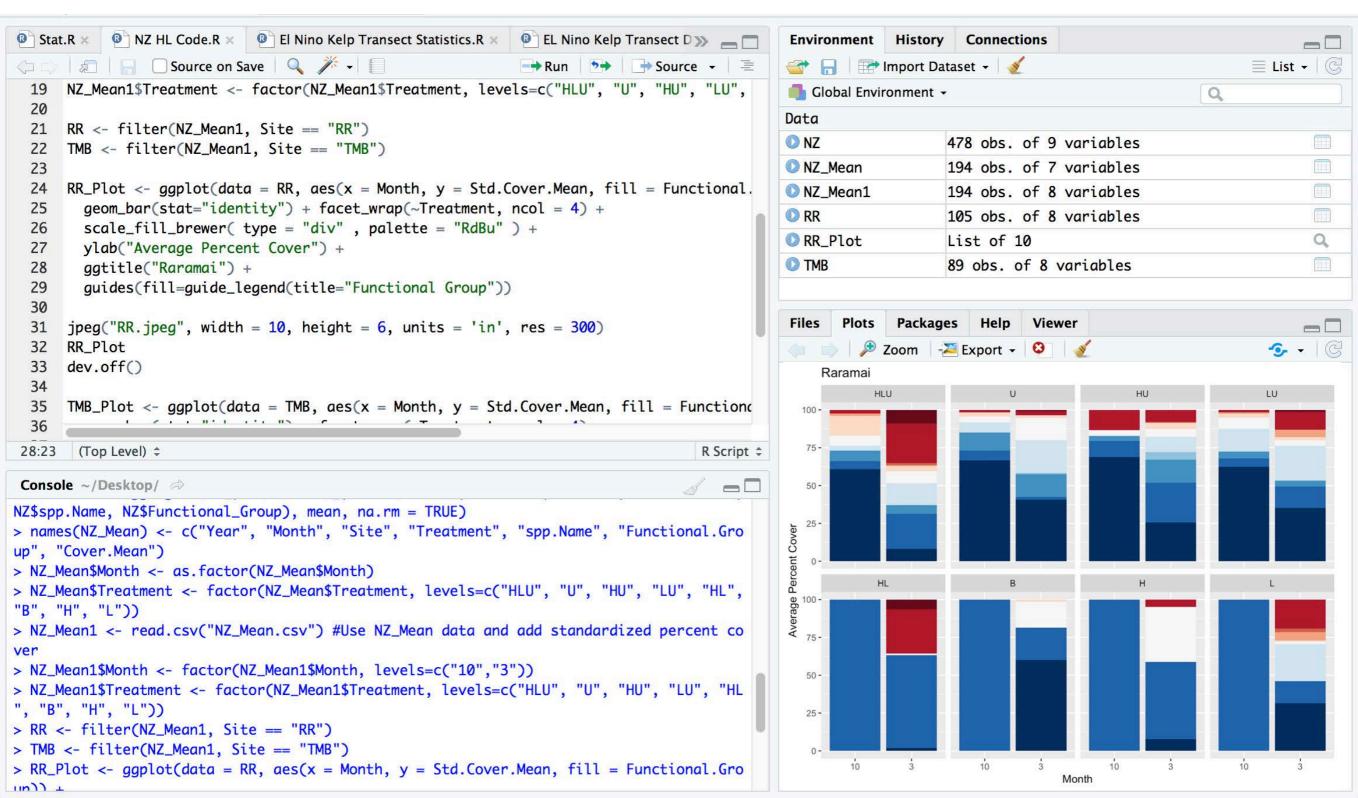




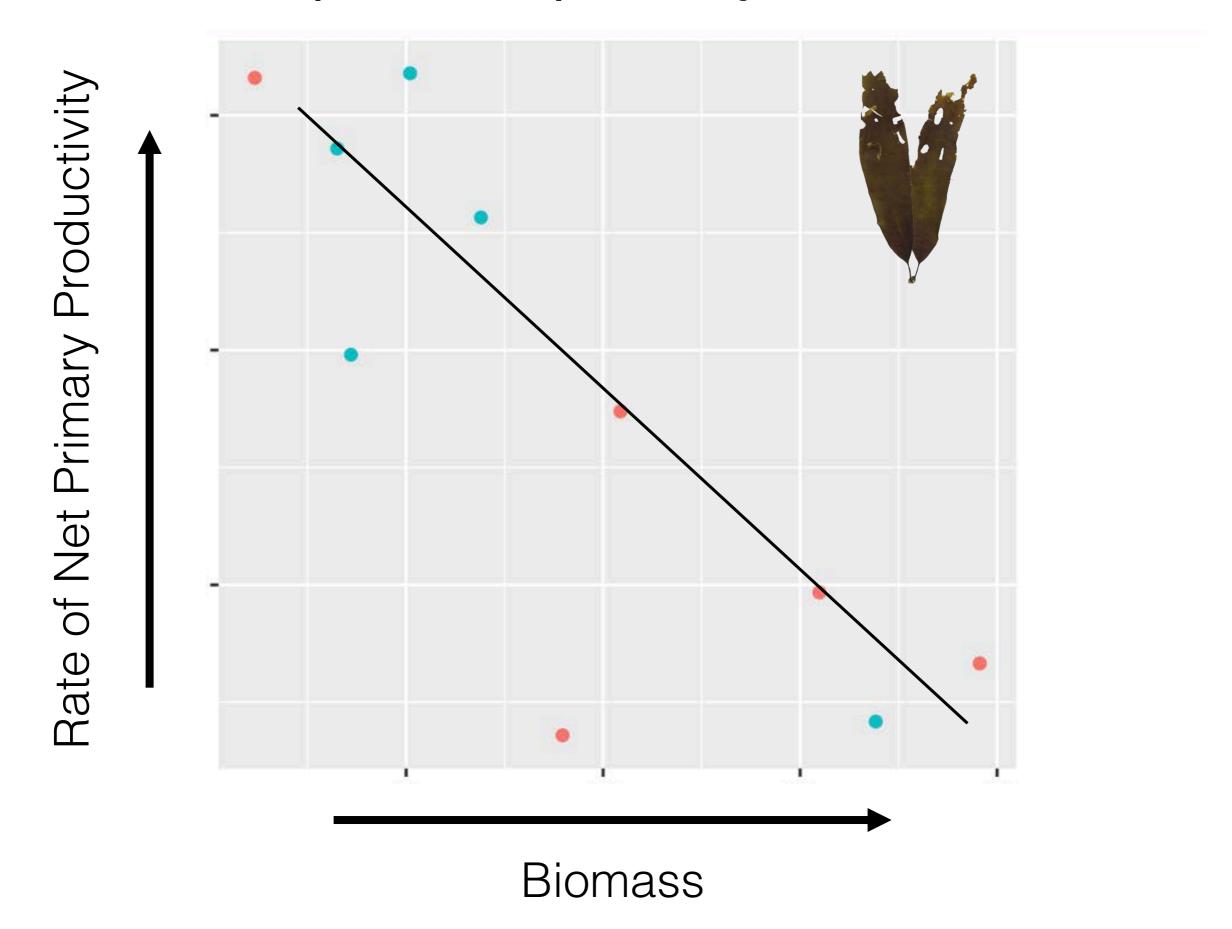






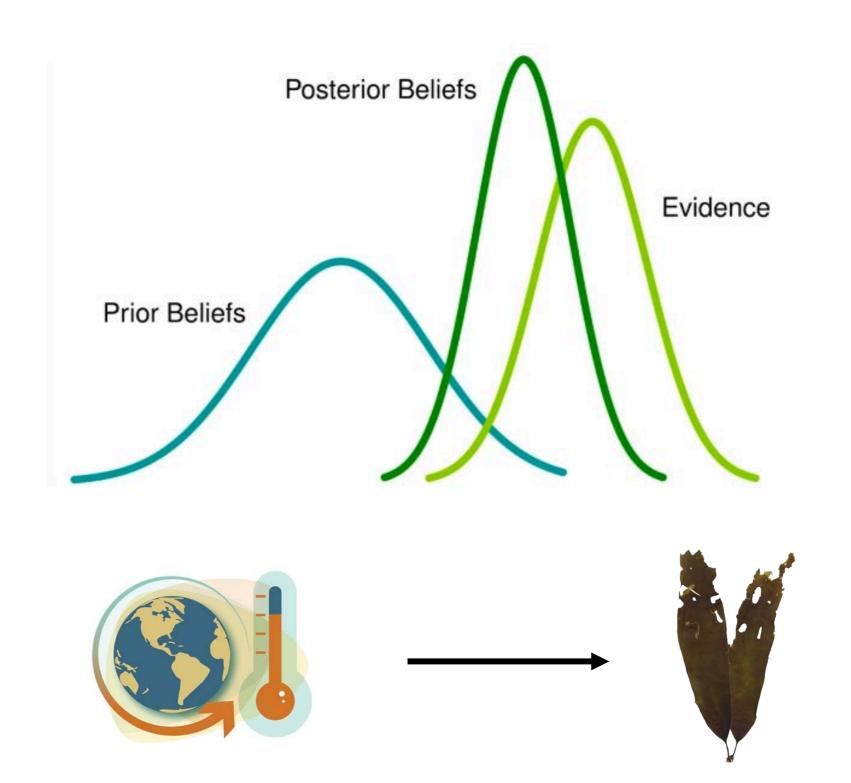


### Size-dependent photosynthesis rate



Bayesian analyses to answer the burning question:

Can we use our past as a predictor for our future?



### Using math to define our natural world

Mathematical modeling allows us to:

- Remove logistical constraints
- Identify uncertainties
- Detect patterns



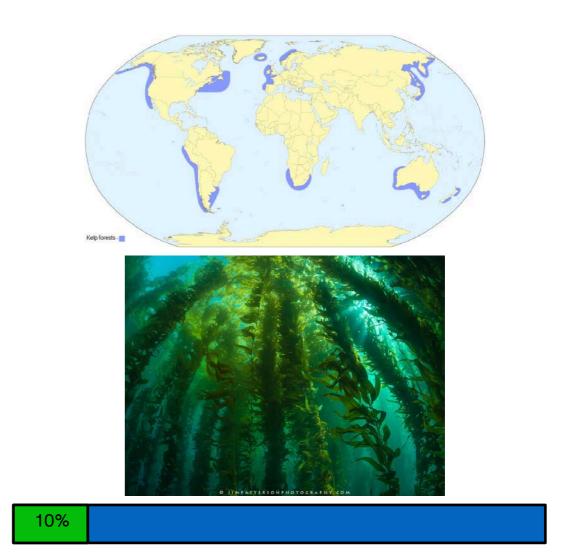




# Kelp Forests

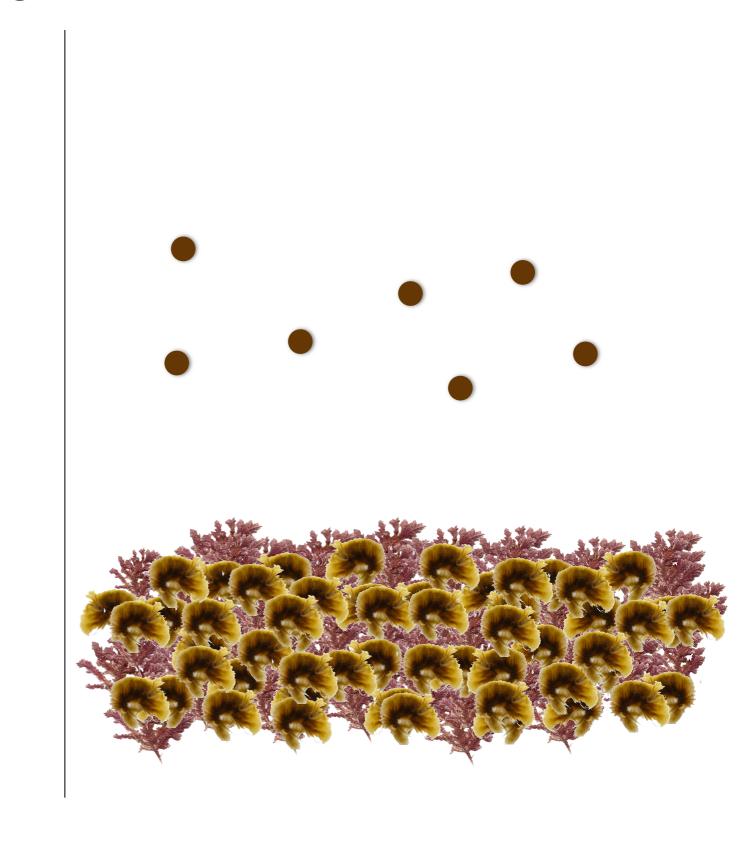


HABITAT AND BREEDING GROUNDS
FOOD SOURCE



OCEANIC PRODUCTION

### Low pH and High Nutrients Scenarios



### Mathematics is not a fixed concept,

but a fluid entity that can be replaced, rearranged, and created with artistry

akin to language.

### Language Manipulation

Oliver looked around, then ran frantically over the bridge, muttering under his breath.

Having looked around, Oliver ran frantically over the bridge, muttering under his breath.

Oliver looked around. Muttering under his breath, he ran frantically over the bridge.

Frantically, he ran over the bridge, muttering under his breath.

### Math Manipulation

$$\frac{d\overline{g}}{dt} = \frac{\sigma_g^2(kt + \epsilon_\theta - \overline{g})}{\sigma_w^2} + \epsilon_{\overline{g}}$$

$$E\left(\frac{d\overline{g}}{dt} \mid \overline{g}\right) = \frac{\sigma_g^2(kt - \overline{g})}{\sigma_w^2}$$

$$V\left(\frac{d\overline{g}}{dt} \mid \overline{g}\right) = \frac{\sigma_g^2}{N_e} + \frac{\sigma_g^4 \sigma_\theta^2}{\sigma_w^4}$$

$$E(r) = r_m - \frac{\sigma_z^2}{2\sigma_w^2} - \frac{k^2 \sigma_w^2}{2\sigma_g^4} - \frac{1}{4N_e} - \frac{\sigma_\theta^2}{2\sigma_w^2} \left( \frac{\sigma_g^2}{2\sigma_w^2} + 1 \right)$$



All other teachers



Math mentor

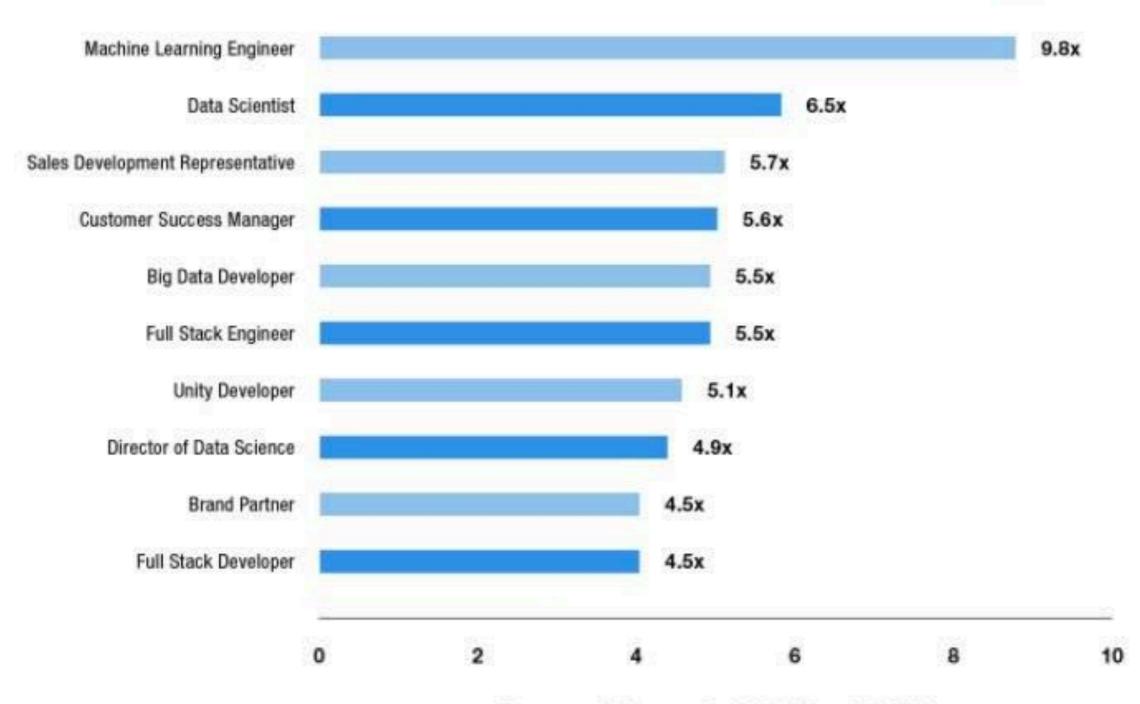


# A world driven by

The importance of meaningful representation, number sense/flexibility, and data fluency.

#### **Top 20 Emerging Jobs**



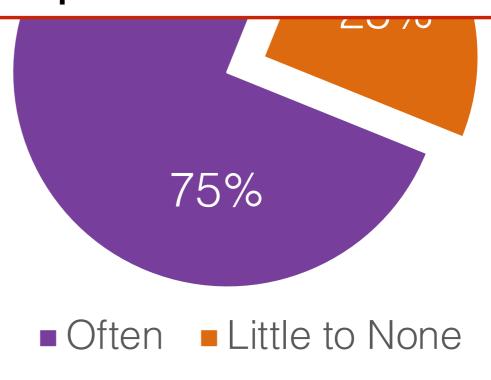


Rate of Growth (2012 - 2017)

Use of Calculus



65% of people say they wished they learned more about how to analyze and interpret data



1 9 119 b ( Singe Sub ( Sin Traditional Math Bin Carl a firey logs from grange of the state of the of eith differ ! Real World

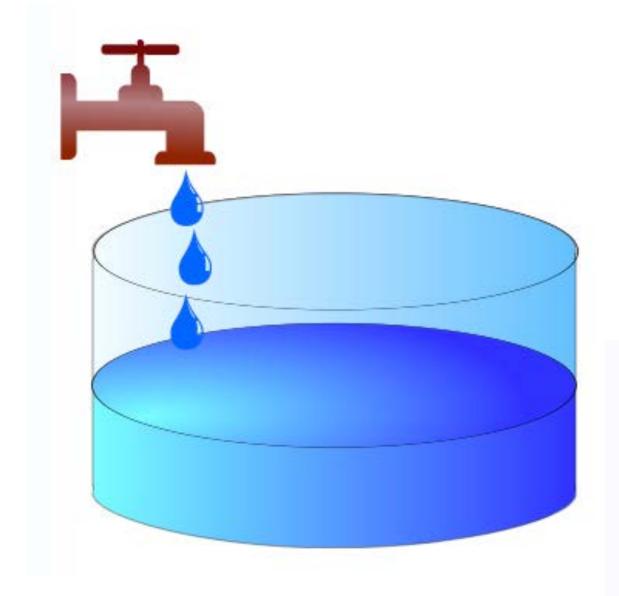
### Meaningful Representation

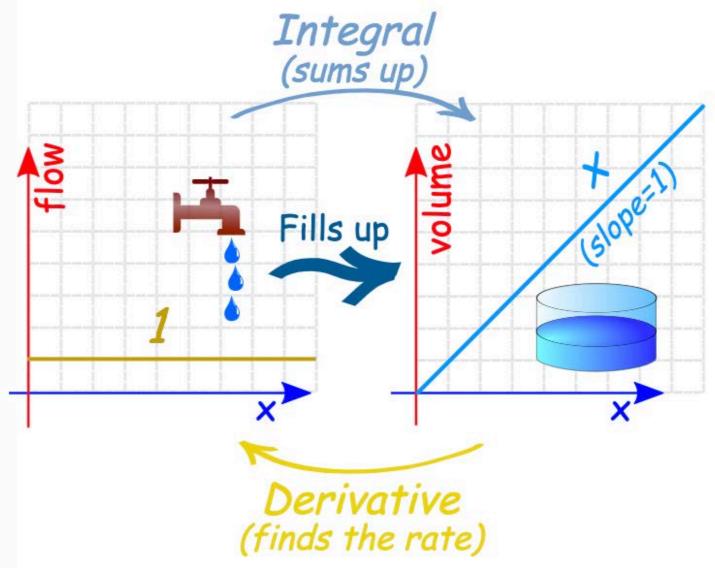
Rationalize the denominator in the equation:

$$\frac{3}{\sqrt{x-7}}$$

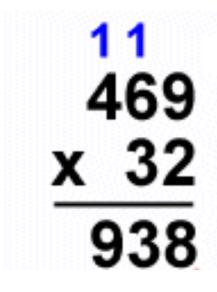
Find the imaginary zeros of the equation:

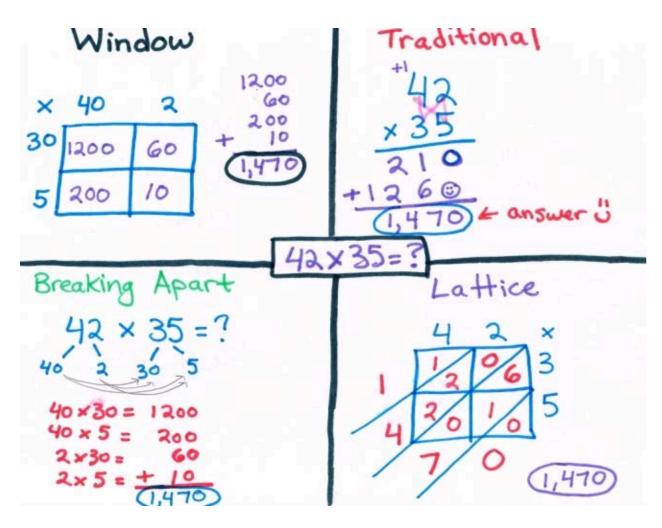
$$f(x) = 4x^4 + 35x^2 - 9$$





## Number Sense/Math Flexibility



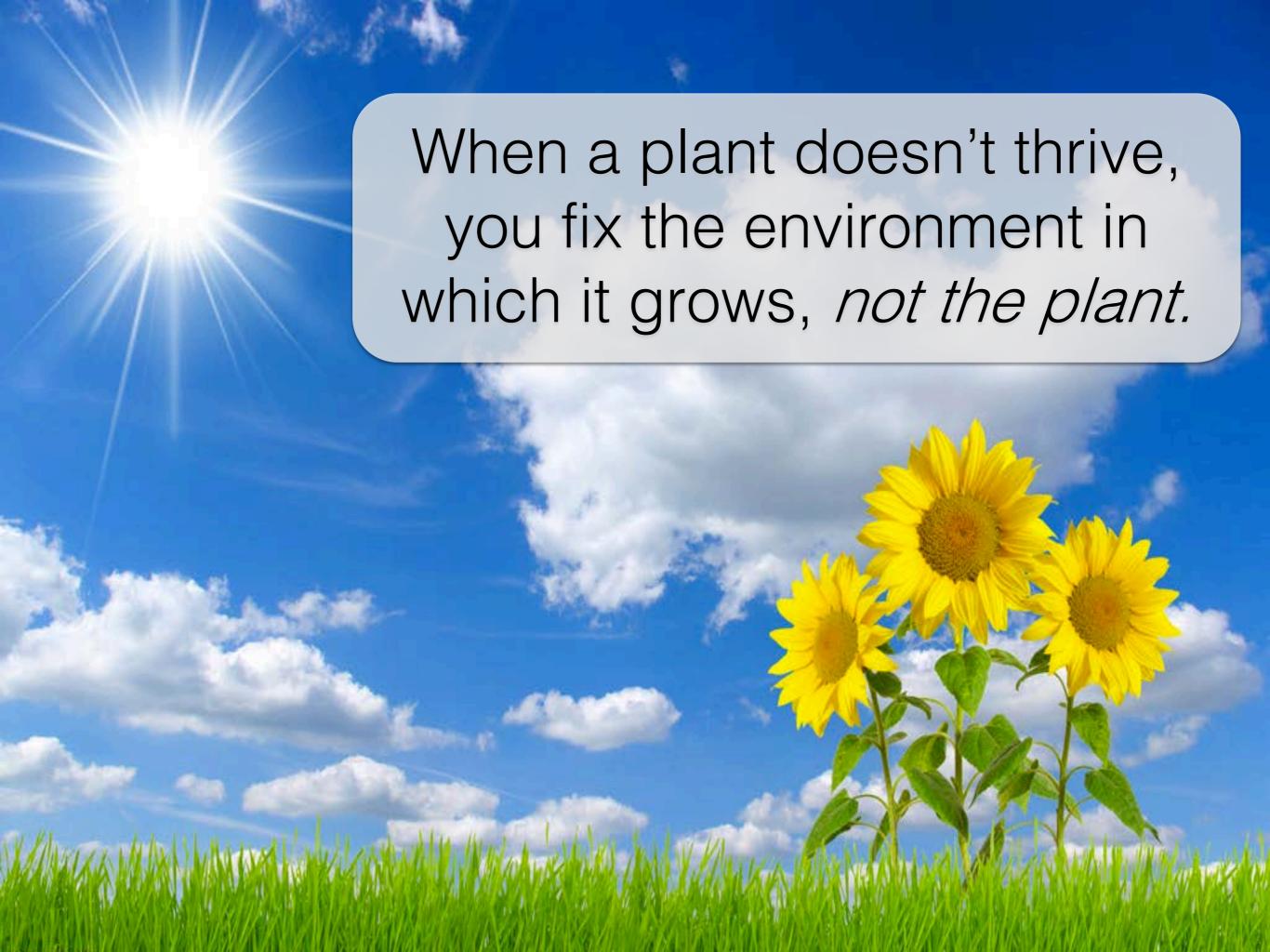


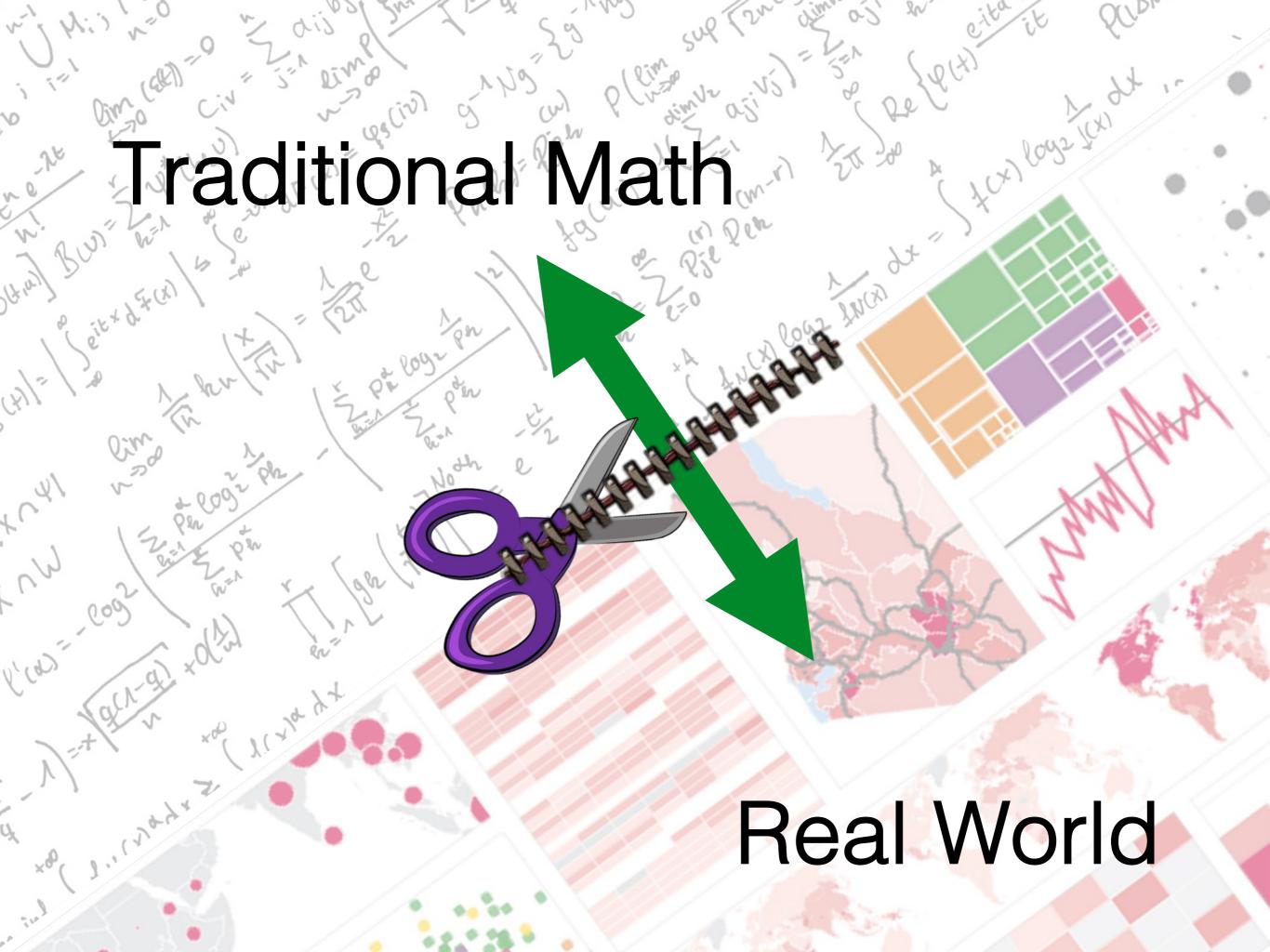


# Data Fluency

Α	В	С	D	E	F	G	Н	I	J	K	L	М			
ountry		_	Area sq mi	Pop. Density,	Coastline (co			GDP (\$/capit	Literacy %	Phones	Arable	Crops			
_	ASIA (EX. NE		647500	48	0			700				0.3			
lbania	EASTERN EU		28748	124.6								4.4			
lgeria	NORTHERN A		2381740		0.04	-0.39									
merican Sa		57794		290.4	58.29	-20.71	9.27	8000							
ndorra	WESTERN EL		468	152.1	0	6.6		19000							
ngola	SUB-SAHARA		1246700		0.13	0		1900				0.3			
nguilla	LATIN AMER			132.1	59.8	10.76	21.03	8600		460	0				
ntigua & Ba	a LATIN AMER	69108	443	156	34.54	-6.15	19.46								
rgentina	LATIN AMER	39921833	2766890	14.4	0.18	0.61	15.18	11200	97.1	220.4	12.31	0.4			
rmenia	C.W. OF IND.	2976372	29800	99.9	0	-6.47	23.28	3500	98.6	195.7	17.55	2			
ruba	LATIN AMER	71891	193	372.5	35.49	0	5.89	28000	97	516.1	10.53				
ustralia	OCEANIA	20264082	7686850	2.6	0.34	3.98	4.69	29000	00	565.5	6.55	0.0			
ustria	WESTERN EL	8192880	83870	97.7	0	2	4.66	30000		452.2	16.91				
zerbaijan	C.W. OF IND.	7961619	86600	91.9	0	-4.9	81.74	3400		137.1	19.63	2.:			
ahamas, Th	LATIN AMER	303770	13940	21.8	25.41	-2.2	25.21	16700		460.6				Month	
ahrain	NEAR EAST	698585	665	1050.5	24.21	1.05	1		egory Category		Cause		2007	Year / Month 2004	
							129 20 100 80 60 40 20 8	Spa	Security Sec	Completes 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	Procedure Crespo Training	Management Extraord Equipment	10 Cone 1		
							Bolto Shele Lincol			Month Jan Feb Mar Apr May Jun Ad Aug Sep Oct		Trend	Naar Mee Medium	) Inca	Design - Equipment   Ecternal   Managem   Manetal   Personnal   Procedure   Taming - evently   Colical   Major







Change will not come if we wait for some other person... or some other time.

We are the ones we've been waiting for.

We are the change that we seek.

- Barack Obama



# QUESTIONS?

